

1 **Thickening mechanism under high compression stress based on**
2 **rheological properties: Comparison between compression effect and**
3 **compression-shear coupling effect**

4 Aixiang Wu ^{1,2)}, Zhenqi Wang ^{1*)}, Zhuen Ruan ^{1,2,4*)}, Raimund Bürger ³⁾, Shaoyong Wang ^{1,4)}, Yi Mo ^{4,5)}

5
6 1) Key Laboratory of the Ministry of Education of China for High-efficient Mining and Safety of Metal
7 Mines, University of Science and Technology Beijing, Beijing 100083, China

8 2) Shunde Innovation School, University of Science and Technology Beijing, Foshan 528399, China

9 3) CI²MA and Departamento de Ingeniería Matemática, Facultad de Ciencias Físicas y Matemáticas,
10 Universidad de Concepción, Casilla 160-C, Concepción, Chile

11 4) School of Civil and Resource Engineering, University of Science and Technology Beijing, Beijing
12 100083, China

13 5) China Railway Construction Tongguan Investment Co., Ltd, Tongling 244000, Anhui, China

14 ***Corresponding authors:** Zhenqi Wang, E-mail: 15101014530@163.com; Zhuen Ruan, E-mail:
15 ustb_ruanzhuen@hotmail.com

16
17 **Abstract:** Tailings thickening is the primary link and key technology of
18 cemented paste backfill (CPB) technology. However, the concentration of
19 thickened tailings often is substandard because of the unclear of thickening
20 mechanism. Therefore, this paper inveterated the thickening mechanism based
21 on the rheological properties of tailings. Firstly, the double yield stress
22 (compressive and shear yield stress) and concentration evolution under
23 compression and compression-shear coupling effects were tested, respectively.
24 And then the correlation analysis between concentration and double yield
25 stress was carried out. The concentration shows a power function of the double
26 yield stress, and shear yield stress is a linear function of the compressive yield
27 stress. It is found that the linear fitting proportional coefficients under the
28 compression effect are lower than those under the compression-shear coupling
29 effect. The full compression stress range is divided into the low and high
30 compression stress ranges and the shear yield stress-compressive yield stress
31 proportional coefficients in the two compression stress ranges are linearly fitted.
32 It is found that the proportional coefficients in the low compression stress range
33 are lower than those in the high compression stress range under the
34 compression effect, but the opposite results are shown under the compression-
35 shear coupling effect, which shows that the introduction of rake-shearing action
36 by the compression-shear coupling effect mainly improves the thickening rate
37 and the thickening effect in the low compression stress range. Moreover, by
38 introducing the rake-shearing action, the concentration growth ratio also
39 confirms that the compression-shear coupling effect improves the thickening
40 effect in the low compression stress range. Furthermore, from the evolution of

41 flocc structure and drainage channels, the thickening mechanism of the
42 compression effect and compression-shear coupling effect was revealed. The
43 results are beneficial for obtaining a satisfied underflow concentration in CPB.
44

45 **Keywords:** High compression stress; Compression-shear coupling effect;
46 Double yield stress; Concentration; Thickening mechanism

47 **1 Introduction**

48 The mining of metal mines causes many security factors, among which the
49 tailings ponds and underground goafs are considered as the two major hazards
50 [1-5]. Cemented paste backfill (CPB) technology is an environmentally friendly,
51 safe, economical and high-efficient mining method that evenly mixes tailings,
52 water and cementitious materials into paste slurry and then backfills it into the
53 underground goafs. This method not only solves the problem of mining safety
54 caused by underground goafs, but also eliminates the environmental pollution
55 and land occupation of tailings ponds, and realizes the "one waste cures two
56 evils" [6-10].

57 The process of CPB technology mainly includes tailings thickening, mixing,
58 pipeline transportation (gravity or pumping), and stope maintenance, in which
59 tailings thickening is the primary link and key technology. Tailings thickening
60 thickens the low-concentration tailings slurry from the mill to form high-
61 concentration paste-like underflow. The deep cone thickener (DCT) will output
62 the high concentration tailings slurry through flocculation, sedimentation,
63 compaction, and thickening in turn with its high-efficiency treatment capacity
64 [15-22], and the thickening process of thickened tailings seriously restricts the
65 throughput and thickening effect. Especially at present, the low ore grade and
66 the mineral processing technology make the tailings particles processed from
67 the mill develop in a finer and finer direction, which brings a series of problems
68 such as difficult flocculation, turbid overflow, difficult thickening, and
69 substandard concentration, which seriously restricts the development of
70 thickening technology [23-25]. The concentration is the most important index to
71 measure the thickening performance. The substandard concentration seriously
72 affects the backfilling operations, which also harms the stability of the CPB
73 structure and the backfilling cost.

74 The low concentration is mainly related to the thickening capacity of the
75 thickener, and the thickening capacity depends on the thickener structure. The
76 thickened tailings will show different thickening mechanisms with the different
77 thickeners, further affecting the concentration. At present, thickeners mainly
78 include ordinary thickener, high-efficiency thickener, and DCT (also called paste
79 thickener) [26-29], among which DCT are widely used in CPB systems, and
80 DCT is developed based on high-efficiency thickener, mainly to increase the
81 compression stress of the thickened tailings and output higher concentration.
82 The two most important factors in the DCT that affect the thickening are mud
83 layer pressure and rake-shearing action. The mud layer pressure inside the
84 DCT is mainly realized by increasing the mud layer height. The rake-shearing

85 action promotes the thickening through low-speed shearing effect, and whether
86 or not the rake-shearing action greatly influences.

87 The research on the thickening mechanism of thickened tailings mainly focuses
88 on the influence of mud layer height, rake-shearing rate, and other aspects. Still,
89 it lacks the research from the angle of internal rheology. Rheology is an
90 important basic theory of tailings thickening, and rheological properties are
91 important internal factors of the concentration evolution. Among them, the
92 thickened tailings of the thickener are under the high mud layer compression
93 and the rake-shearing action, and it has the properties of compressive
94 resistance and shearing resistance, showing the rheological properties of
95 compressive yield stress and shear yield stress [30-37].

96 The research on thickening of thickened tailings mainly focuses on settling
97 column tests and small-scale dynamic thickening simulation experiments [38-
98 41]. These conventional indoor thickening experiments can only obtain
99 concentration and rheological properties under the condition of low mud layer
100 compression stress (<1 kPa), which is far from the high mud layer compression
101 stress (5-100 kPa) of the industrial thickener, and has certain limitations on
102 thickening mechanism. It is necessary to the thickening mechanism of
103 thickened tailings with high compression stress.

104 The thickening process of thickened tailings is essentially a dynamic evolution
105 process of flocs and drainage channels. A large number of studies have made
106 micro-analysis (such as Computed Tomography (CT), Scanning Electron
107 Microscope (SEM), and Focused Beam Reflectance Measurement (FBRM)) on
108 tailings flocs and drainage channels, among which the theory of floc-shearing
109 densification is put forward for the evolution of flocs under rake-shearing action
110 [42-49]. Therefore, it is also necessary to investigate the thickening mechanism
111 of thickened tailings from the perspective of the evolution of flocs and drainage
112 channels.

113 In this study, the concentration and double yield stress evolution in the high
114 compression stress (0-30 kPa) was tested by a self-developed compression-
115 shear coupling experimental device, and the correlation between concentration
116 and double yield stress was characterized, respectively. The thickening
117 mechanism of thickened tailings was analyzed from the double yield stress
118 relationship, concentration growth ratio, and the microscopic evolution of flocs
119 and drainage channels.

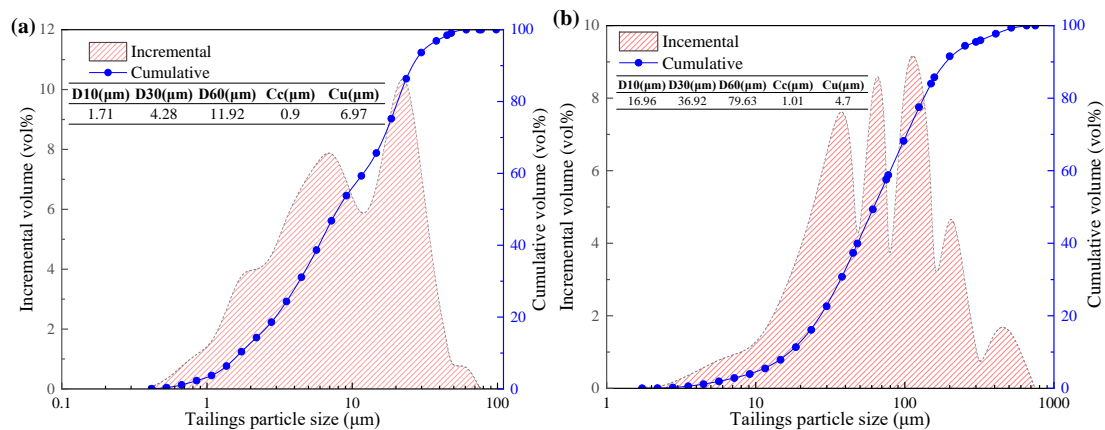
120 **2 Materials and methods**

121 **2.1 Raw materials**

122 **2.1.1 Tailings**

123 The tailings used in this study come from a lead-zinc mine. The tailings are
124 divided into classified tailings and fine-grained tailings by hydrocyclone. The
125 unclassified tailings are composed of 30 wt% fine-grained tailings and 70 wt%
126 classified tailings. The influencing factors of different fine-grained tailings
127 contents are studied by changing the content of fine-grained tailings. Because
128 the tailings particle size is ultra-fine, the fine-grained tailings and classified

129 tailings are analyzed by Omece TopSizer laser particle size analyzer [8,10]. The
 130 tailings particle size distribution and characteristic particle size of fine-grained
 131 tailings and classified tailings are shown in Fig. 1.
 132 As can be seen from Figures 1(a) and 1(b), the particle size of fine-grained
 133 tailings is less than 100 μm , the particle size of tailings is in the range of 0.1-60
 134 μm , the proportion less than 10 μm is more than 50 vol%, and the C_c (0.9)
 135 is less than 1, so it belongs to fine-grained tailings. The particle size of classified
 136 tailings is in the range of 1-400 μm , and the proportion of tailings larger than
 137 100 μm is more than 30 vol%, and C_u is less than 5, so it belongs to coarse-
 138 grained tailings.



139

140

Fig. 1 Particle size distribution: (a) Fine-grained tailings; (b) Classified tailings

141

142

143

144

145

146

147

148

149

150

151

152

153

154

The specific gravity of fine-grained tailings and classified tailings was tested by the pycnometer method. The specific gravity of fine-grained tailings is 3.063, and that of classified tailings is 3.008. The porosity and specific surface area of fine-grained tailings and classified tailings were analyzed. The loose porosity of fine-grained tailings is 67.14%, the dense porosity is 59.09%, and the specific surface area is 1405.60 $\text{m}^2 \cdot \text{kg}^{-1}$. The loose porosity of classified tailings is 52.52%, the dense porosity is 40.16%, and the specific surface area is 172.86 $\text{m}^2 \cdot \text{kg}^{-1}$.

X-ray fluorescence (XRF) was used to analyze the main chemical composition of fine-grained tailings and classified tailings, and the analysis results are shown in Table 1. Both fine-grained tailings and classified tailings contain high contents of CaO and MgO, indicating that tailings contain more minerals, such as dolomite and calcite.

Table 1 Chemical composition of fine-grained tailings and classified tailings

	CaO	MgO	SiO ₂	Al ₂ O ₃	Fe	S	Zn	Pb
Fine-grained tailings / wt%	38.62	6.63	6.17	2.8	2.29	2.02	1.05	0.96
Classified tailings / wt%	31.26	12.45	4.68	1.79	2.97	1.25	2.43	1.17

155

2.1.2 Flocculant and water

156

157

158

In this study, the flocculants suitable for tailings flocculation and thickening are selected, which are produced by SNF Company, including a cationic polyacrylamide (350E), a nonionic polyacrylamide (6003S) and three anionic

159 polyacrylamides (625S, 645th and 665S). The main difference among the three
160 polyacrylamides is the different molecular weights, of which 665S is the highest,
161 followed by 645S and 625S.

162 The flocculant was selected by settling column experiments. The feeding
163 concentration of unclassified tailings is 15 wt%, the flocculant dosage is 20 g t⁻¹
164 and the flocculant dosage is 0.1 wt%. The height of the solid-liquid interface
165 was recorded and the initial settling rate was obtained (0-60 s solid-liquid
166 interface height fitted straight line slope). The initial settling rates corresponding
167 to flocculant types 625S, 645S, 665S, 350E, and 6003S are 2.00 mm·s⁻¹, 2.22
168 mm·s⁻¹, 1.31 mm·s⁻¹, 1.00 mm·s⁻¹, and 1.34 mm·s⁻¹, respectively. The
169 concentration of the thickened tailings settled for 24 h was tested. The
170 concentrations corresponding to 625S, 645S, 665S, 350E and 6003S are 44.40
171 wt%, 48.54 wt%, 38.61 wt%, 31.99 wt%, and 36.96 wt%, respectively, among
172 which anionic polyacrylamide 645S has the highest initial settling rate and
173 concentration, so anionic polyacrylamide 645S is selected as the flocculant
174 used in the experiments.

175 The experimental water in this study is filtered tap water in the laboratory, and
176 its pH is 7.0.

177 2.2 Experimental methods

178 These research experiments are divided into three stages, as shown in Fig. 2.
179 Firstly, the flocculation condition optimization experiment was carried out, then
180 the dynamic thickening experiment, and finally, the rheological properties and
181 concentration under the compression and compression-shear coupling effects
182 were tested.

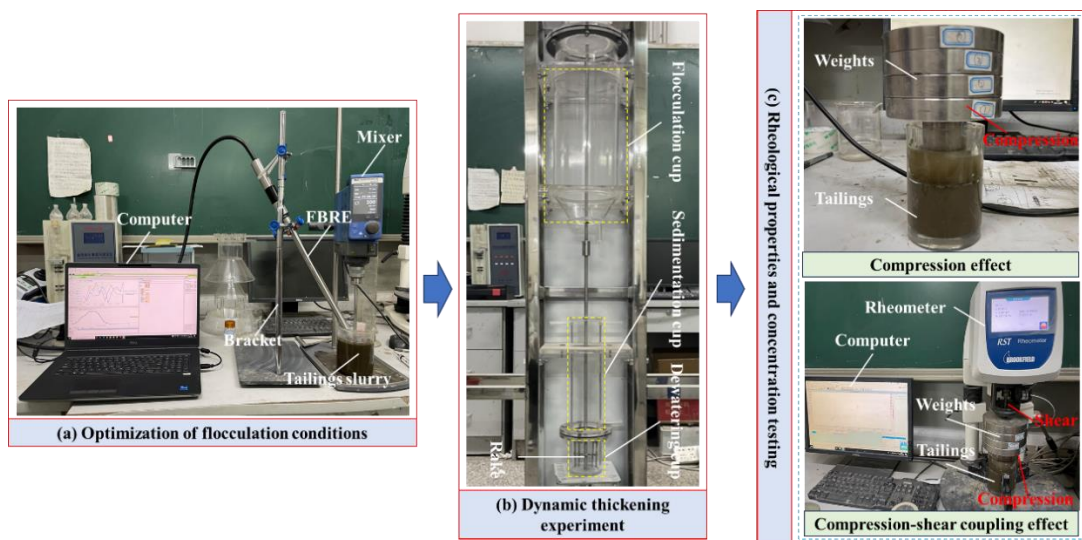


Fig. 2 Experimental procedure

183
184

185 2.2.1 Optimization experiment of flocculation conditions

186 As shown in Fig. 2(a), the mean weighted chord length (MWCL) of flocs in the
187 flocculation process was tested using this experimental device, and the
188 sedimentation characteristics were studied to obtain the concentration under
189 different flocculation conditions. The experiment(a) adopted the Box-Behnken
190 Design (BBD) experimental method. Taking tailings feeding concentration,

191 flocculant solution concentration, shear rate, and shear time as experimental
 192 factors, the tailings feeding concentration range is 10-25 wt%, flocculant
 193 solution concentration range is 1-10 wt‰, shear rate range is 80-400 r·min⁻¹
 194 and shear time range is 30-150 s. The time-ending MWCL and concentration
 195 were taken as the response values to optimize the flocculation conditions, and
 196 there were 29 experimental groups (the experimental scheme is shown in Table
 197 2). The specific experimental process is as follows:

198 (1) Tailings slurry was prepared according to the experimental scheme in Table
 199 2. The mixer (IKA EUROSTAR 60 digital) was used for shearing at the specified
 200 speed, and then the tailings floc size evolution was tested by FBRM. In this
 201 study, the portable Particle Track G400 testing device was used for data
 202 collection and transformation with iC FBRM software, and the sampling period
 203 was set to 2s to test the tailings floc size evolution within the specified shearing
 204 time.

205 (2) Put the tailings slurry tested by FBRM into a 1000 ml measuring cylinder for
 206 settling column experiments. After settling for 24 h, test the concentration of
 207 different experimental groups.

208 The MWCL and concentration corresponding to different experimental groups
 209 shown in Table 2 are finally obtained through the above experiments. The
 210 optimal flocculation conditions are obtained using the "Optimization" function in
 211 Design Expert software, with the maximum concentration and MWCL as the
 212 goals. Finally, the optimal flocculation conditions are as follows: tailings feeding
 213 concentration is 17.05 wt%, flocculant solution concentration is 1.00 wt‰,
 214 shear rate is 166.11 r·min⁻¹, and shear time is 30 s. Under these optimal
 215 conditions, the theoretical concentration is 58.48 wt%, and the MWCL of the
 216 floc is 299.694 μm.

217 Table 2 Flocculation conditions optimization experimental scheme and results

No.	TFC (wt%)	FSC (wt‰)	SR (r·min ⁻¹)	ST (s)	MWCL (μm)	Concentration (wt%)
1	25	5.5	400	90	32.123	35.8254
2	17.5	1	400	90	106.831	44.0545
3	17.5	5.5	240	90	236.357	45.1704
4	10	5.5	400	90	187.602	51.1485
5	17.5	10	400	90	121.315	43.9588
6	17.5	10	240	150	202.028	49.4854
7	10	10	240	90	251.134	59.5803
8	17.5	5.5	240	90	236.357	45.1742
9	10	1	240	90	185.378	54.4317
10	17.5	5.5	240	90	236.357	45.1742
11	17.5	5.5	400	150	94.608	40.2739
12	17.5	5.5	80	150	132.971	52.8526
13	25	5.5	80	90	134.008	43.6431
14	17.5	5.5	240	90	236.357	45.1742
15	10	5.5	80	90	128.945	56.0921
16	17.5	10	80	90	118.342	50.0475

17	10	5.5	240	150	99.303	54.7166
18	25	10	240	90	71.185	33.7223
19	25	5.5	240	150	84.825	36.1826
20	17.5	1	240	150	144.761	46.4598
21	17.5	1	80	90	182.309	55.0657
22	17.5	1	240	30	302.471	56.3792
23	17.5	10	240	30	226.213	45.2413
24	10	5.5	240	30	278.657	55.548
25	17.5	5.5	400	30	209.042	46.2535
26	17.5	5.5	240	90	236.357	45.1742
27	25	1	240	90	150.314	47.6158
28	25	5.5	240	30	195.722	44.9131
29	17.5	5.5	80	30	207.708	52.3361
Optimal results	17.05	1.00	166.11	30	299.694	58.4800

2.2.2 Dynamic thickening experiment

As shown in Fig. 2(b), a three-stage dynamic flocculation thickening experimental device was used to carry out the dynamic thickening experiment. The experimental device consists of a flocculation cup, sedimentation cup and thickening cup from top to bottom, and the concentration is improved by the rake shearing at low speed. The device was used to carry out dynamic thickening experiments under different flocculant dosages and fine-grained tailings contents to obtain high-concentration underflow and provide raw materials for rheological properties and concentration tests. Among them, the flocculant dosage levels are 10, 15, 20, 25, and 30 g t⁻¹, and the fine-grained tailings content is realized by changing the content of fine-grained tailings, which is divided into five levels: 10, 20, 30, 40, and 50 wt%. Other experimental conditions are carried out with the optimal flocculation conditions obtained in section 2.2.1. The experimental scheme of the dynamic thickening experiment is shown in Table 3.

Table 3 Experimental scheme of the dynamic thickening experiment

TFC (wt%)	FSC (wt‰)	SR (r·min ⁻¹)	ST (s)	Flocculant dosage (g t ⁻¹)	Fine-grained tailings content (wt%)
17	1	167	30	20	10, 20, 30, 40, 50
17	1	167	30	10, 15, 20, 25, 30	30

2.2.3 Rheological properties and concentration test

The traditional indoor settling column experiment and small-scale dynamic thickening experiment can only study the thickening behavior of thickened tailings under low compression stress (<1 kPa) [11,17,19], and there is a lack of research on rheological properties and concentration of thickened tailings during thickening under high compression stress and rake-shearing action. Therefore, in this study, the concentration and rheological properties of thickened tailings under compression and compression-shear coupling effects with high compression stress were studied.

As shown in Fig. 2(c), in this experiment, the rheological properties and concentration tests of thickened tailings obtained by the dynamic thickening

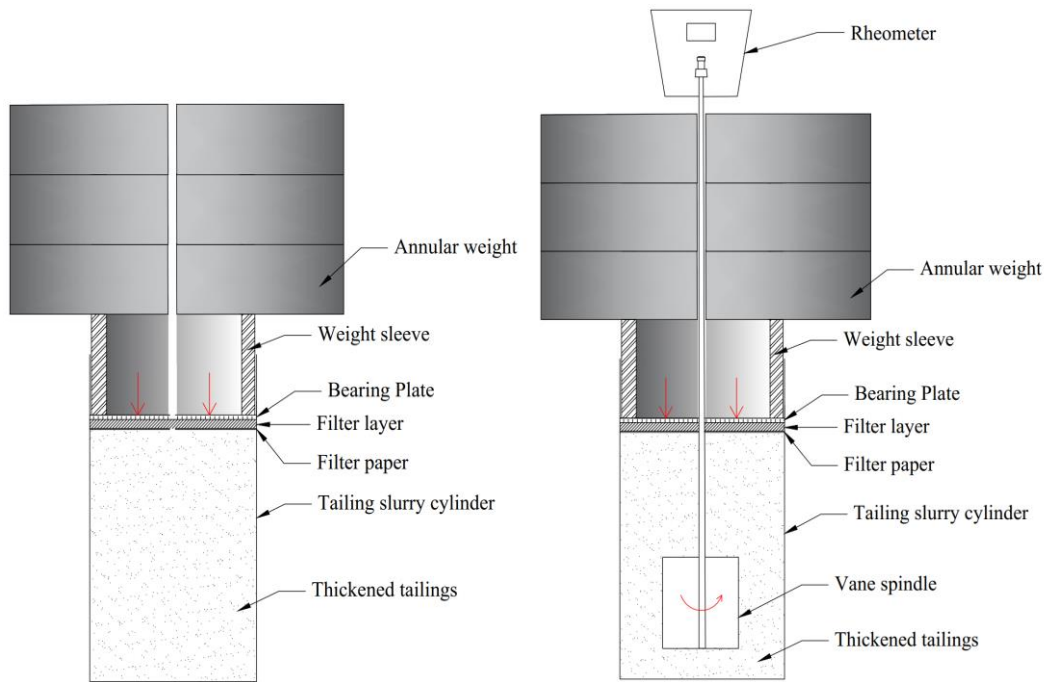
245 experiment in Fig. 2(b) were tested under the effects of compression and
246 compression-shear coupling, respectively (Fig. 3), and finally, the compressive
247 yield stress, shear yield stress and concentration evolution under different
248 flocculant dosages and fine-grained tailings contents were tested. The main
249 difference between the compression effect and compression-shear coupling
250 effect is whether there is a low-speed rake-shearing action. This experiment
251 also lays a physical foundation for revealing the rake-shearing thickening
252 mechanism.

253 (a) Compression effect

254 As shown in Fig. 3(a), the compression effect mainly simulates the thickening
255 behavior of the thickened tailings (high mud layer pressure in the DCT) of the
256 rakeless DCT. The overlying compression stress of the thickened tailings is
257 increased by increasing weights. The weights are made of stainless steel, and
258 the weight sleeve controls the weights to keep the vertical state. Under the
259 weights, there are bearing plate (acrylic material with holes), filter layer (EPE),
260 and filter paper (Whatman Grade2 medium-speed), and the gravity of the
261 weights is equivalent to compressive yield stress. Five pressure levels (C1: 2.55
262 kPa; C2: 8.66 kPa; C3: 14.78 kPa; C4: 20.89 kPa; C5: 27 kPa), each
263 compression stress level is applied for 30 min, the seepage water is sucked out
264 and weighed in time, the concentration of each compression stress level is
265 calculated, and the shear yield stress corresponding to each compression
266 stress level is tested by Brookfield R/S plus rheometer (CSR testing method:
267 0~120 s: 0~120 s⁻¹; 120~240 s: 120~0 s⁻¹).

268 (b) Compression-shear coupling effect

269 As shown in Fig. 3(b), the compression-shear coupling effect mainly simulates
270 the dewatering behavior of the thickened tailings of the DCT with rake-shearing
271 action. Compression stress is applied to the thickened tailings by the weights,
272 and rake-shearing action is applied to the tailings slurry by the vane spindle
273 (VT-40-20) of the rheometer to realize the coupling effect of compression and
274 rake shearing. The shear rate of the vane is 2 r·min⁻¹, and the compression
275 stress testing procedure is the same as above. Finally, concentration and
276 rheological properties can be obtained.



(a) Compression effect

(b) Compression-shear coupling effect

Fig. 3 Rheological properties and concentration testing device

277

278

279

280

3 Results and discussion

281

3.1 Evolution of concentration and rheological properties

282

3.1.1 Evolution of concentration and rheological properties with different flocculant dosages

283

284

The concentration-double yield stress evolution under compression effect with different flocculant dosages is shown in Fig. 4. The concentrations of different flocculant dosages increase rapidly at first and then slow down with the linear growth of compressive yield stress, and the growth rate ($5.89, 4.68, 4.64, 2.26, 3.83 \text{ \%} \cdot \text{kPa}^{-1}$) is higher in the low compressive yield stress range ($0-2.55 \text{ kPa}$) than that ($0.63, 0.58, 0.62, 0.71, 0.50 \text{ \%} \cdot \text{kPa}^{-1}$) in the high compressive yield stress range ($2.55-27 \text{ kPa}$). The maximum concentration corresponding to the maximum compressive yield stress (27 kPa) is 69.47 wt\% (flocculant dosage is 10 g t^{-1}). The shear yield stress shows a linear growth trend with increased compressive yield stress. The maximum shear yield stress is 302.81 Pa (flocculant dosage is 25 g t^{-1}), and the concentration also shows a trend of rapid growth at first and then slow with the increase of shear yield stress.

285

286

287

288

289

290

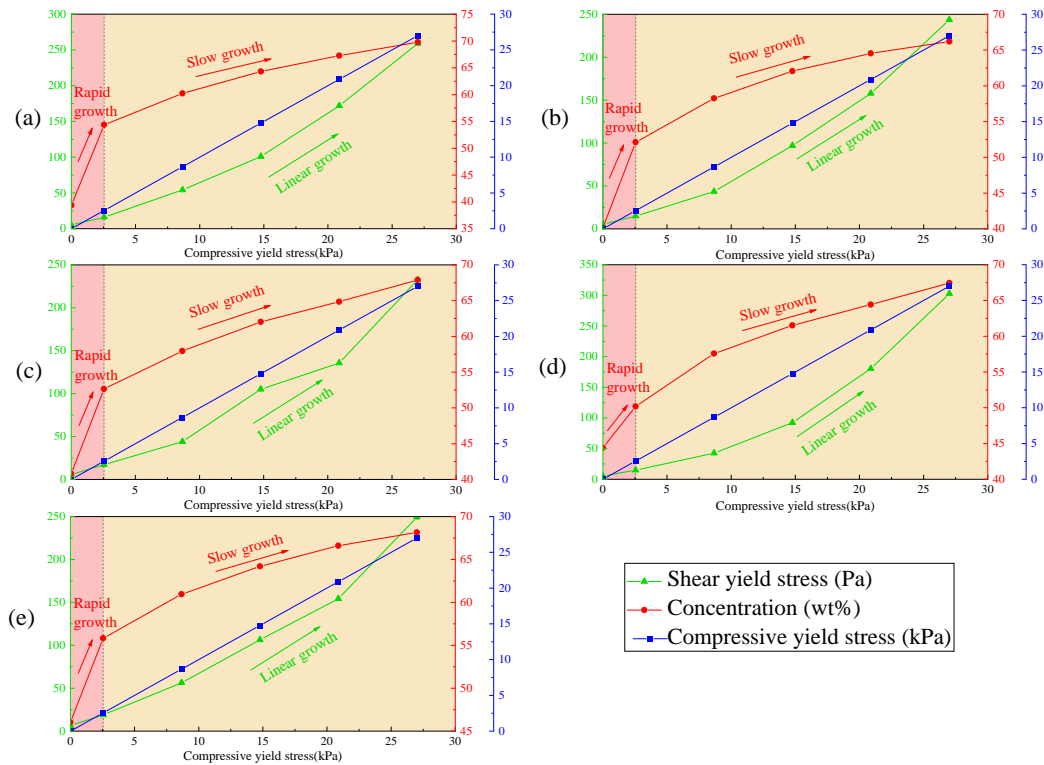
291

292

293

294

295



296

297

298

299

300

301

302

303

304

305

306

307

308

309

310

311

312

313

314

315

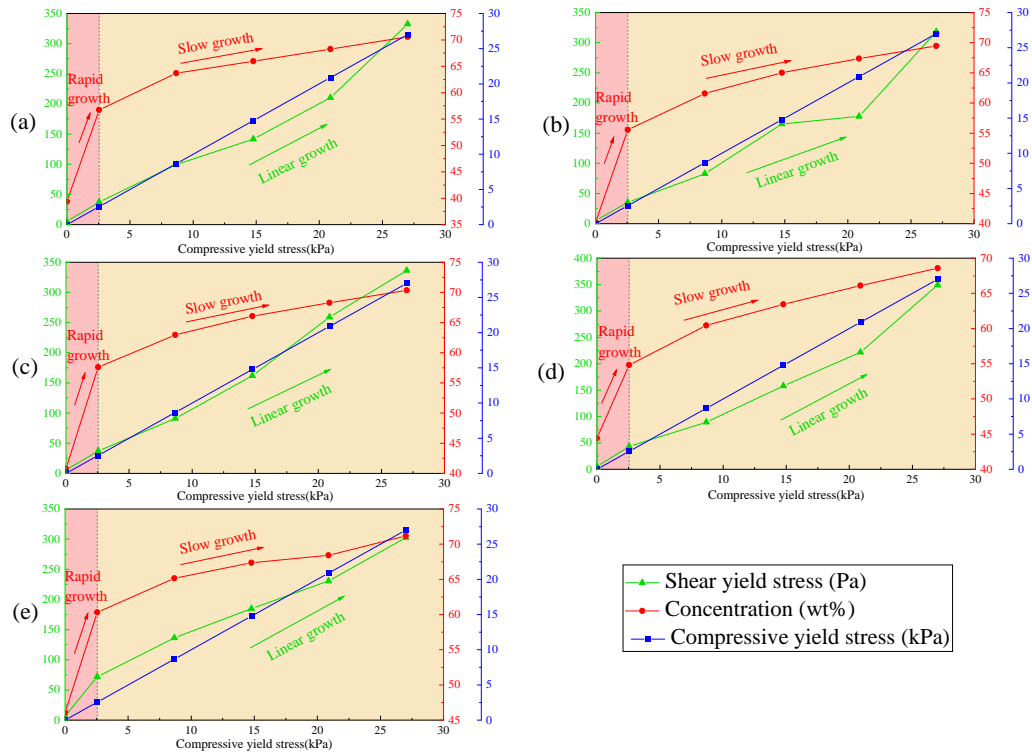
316

317

318

Fig. 4 Evolution of concentration-double yield stress under compression effect with different flocculant dosages: (a) 10 g t⁻¹; (b) 15 g t⁻¹; (c) 20 g t⁻¹; (d) 25 g t⁻¹; (e) 30 g t⁻¹

Fig. 5 shows the evolution of the concentration-double yield stress under the compression-shear coupling effect with different flocculant dosages. The concentrations of different flocculant dosages increase rapidly at first and then slow down with the linear growth of compressive yield stress. The growth rate (6.81, 6.04, 6.59, 4.08, and 5.60 %·kPa⁻¹) is higher in the low compressive yield stress range than that in the high compressive yield stress range (0.57, 0.57, 0.52, 0.56, 0.44 %·kPa⁻¹). Moreover, the concentration growth rate in the low compressive yield stress range under compression-shear coupling effect is higher than that under the compression effect, but in the high compressive yield stress range, the opposite is true. The maximum concentration is 71.18 wt% (flocculant dosage is 30 g t⁻¹), and the concentration is greatly improved compared with the compression effect, which shows that the thickening effect under the compression-shear coupling effect is better than that under the compression effect. The shear yield stress shows a linear growth trend with increased compressive yield stress. The shear yield stress under the compression-shear coupling effect is greater than that under the compression effect. The maximum shear yield stress is 349.24 Pa (flocculant dosage is 25 g t⁻¹), and the maximum shear yield stress is higher than that under compression effect. With the increase of shear yield stress, the concentration also shows a trend of rapid growth at first and then slow.

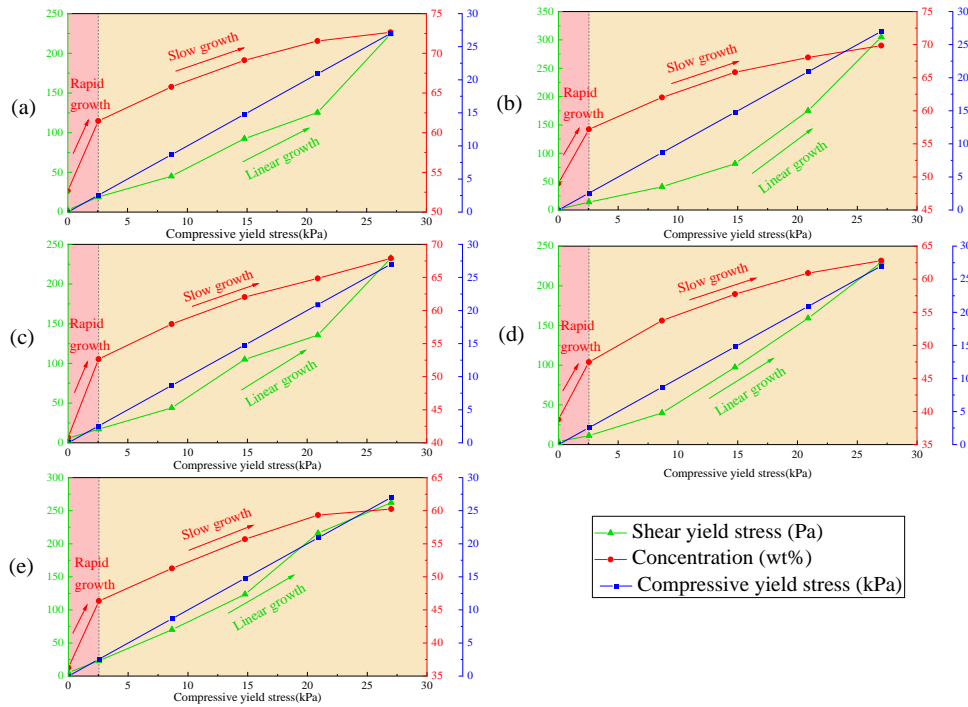


319

320 Fig. 5 Evolution of concentration-double yield stress under compression-shear coupling effect
 321 with different flocculant dosages: (a) 10 g t⁻¹; (b) 15 g t⁻¹; (c) 20 g t⁻¹; (d) 25 g t⁻¹; (e) 30 g t⁻¹

322 **3.1.2 Evolution of concentration and rheological properties with different**
 323 **fine-grained tailings contents**

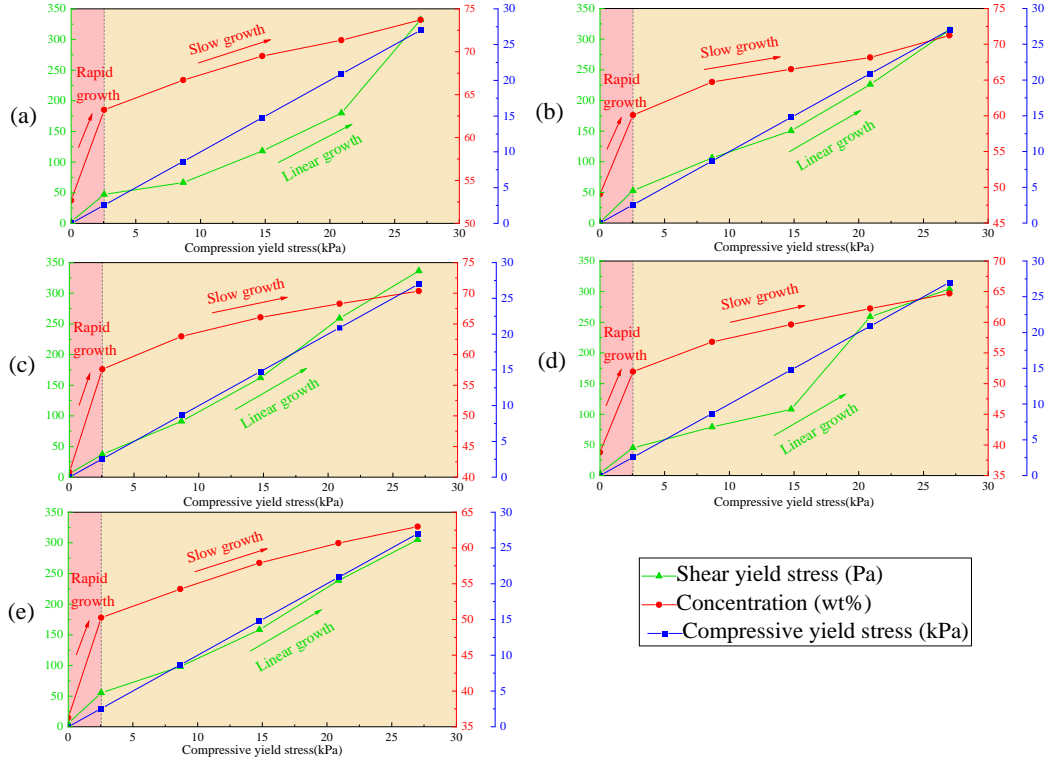
324 The evolution of the concentration-double yield stress under compression effect
 325 with different fine-grained tailings contents is shown in Fig. 6. The
 326 concentrations of different fine-grained tailings contents increase rapidly at first
 327 and then slow down with the linear growth of compressive yield stress, and the
 328 growth rate (3.46, 3.21, 4.64, 3.41 and 3.96 %·kPa⁻¹) is higher in the low
 329 compressive yield stress range than that in the high compressive yield stress
 330 range (0.46, 0.52, 0.62, 0.63 and 0.57 %·kPa⁻¹). The maximum concentration
 331 corresponding to different fine-grained tailings content levels is 72.65, 69.86,
 332 67.90, 62.81, and 60.26 wt%, respectively. It can be seen that with the growth
 333 of fine-grained tailings content, the concentration decreases. With the increase
 334 of compressive yield stress, shear yield stress shows a linear growth trend, and
 335 the maximum shear yield stress is 305.07 Pa (fine-grained tailings content is
 336 20 wt%), and the concentration also shows a trend of rapid growth at first and
 337 then slow with the increase of shear yield stress.



338

339 Fig. 6 Evolution of concentration-double yield stress under compression effect with different
 340 fine-grained tailings contents: (a) 10 wt%;(b) 20 wt%;(c) 30 wt%;(d) 40 wt%;(e) 50 wt%

341 Fig. 7 shows the evolution of the concentration-double yield stress under the
 342 compression-shear coupling effect with different fine-grained tailings contents.
 343 The concentrations of different fine-grained tailings contents increase rapidly at
 344 first and then slow down with the linear growth of compressive yield stress. The
 345 growth rate ($4.15, 4.34, 6.59, 5.17, \text{ and } 5.49 \text{ \%} \cdot \text{kPa}^{-1}$) in the low compressive
 346 yield stress range is higher than that ($0.43, 0.46, 0.52, 0.52 \text{ \%} \cdot \text{kPa}^{-1}$) in the high
 347 compressive yield stress range. Moreover, the growth rate of concentration in
 348 the low compressive yield stress range under the compression-shear coupling
 349 effect is higher than that under the compression effect, but in the high
 350 compressive yield stress range, the opposite is true. The maximum
 351 concentrations corresponding to different fine-grained tailings contents are
 352 $73.71, 71.23, 70.35, 64.71, \text{ and } 62.99 \text{ wt\%}$, respectively. It can be seen that
 353 with the growth of fine-grained tailings content, the concentration decreases,
 354 and the concentration corresponding to different fine-grained tailings contents
 355 under the compression-shear coupling effect is higher than that under
 356 compression effect, which shows that the thickening effect under compression-
 357 shear coupling effect is better than that under compression effect. The shear
 358 yield stress shows a linear growth trend with increased compressive yield stress.
 359 The shear yield stress under the compression-shear coupling effect is greater
 360 than that under the compression. The maximum shear yield stress is 336.54 Pa
 361 (fine-grained tailings content is 30 wt\%), and the maximum shear yield stress
 362 is higher than that under compression effect (growth ratio: 10.32%). With the
 363 increase of shear yield stress, the concentration also shows a trend of rapid
 364 growth at first and then slow.



365

366

Fig. 7 Evolution of concentration-double yield stress under compression-shear coupling effect with different fine-grained tailings contents: (a) 10 wt%;(b) 20 wt%;(c) 30 wt%;(d) 40 wt%;(e)

367

368

50 wt%

369

3.2 Correlation analysis

370

3.2.1 Concentration-shear yield stress

371

The evolution of concentration and double yield stress in Section 3.1 shows that the concentration increases rapidly at first and then slowly with the linear growth of shear yield stress and compressive yield stress. The relationship between concentration, shear yield stress, and compressive yield stress under the compression and compression-shear coupling effects with different flocculant dosages and fine-grained tailings contents was characterized and analyzed, respectively. It is found that the relationship between concentration and shear yield stress and compressive yield stress is a power function, and the formulas are shown in Eq. (1) and Eq. (2).

379

380

$$U_{\text{Flocculant condition}} = m \cdot \tau^n \quad (1)$$

381

Where $U_{\text{Flocculant condition}}$ represents the concentration under different flocculant conditions, wt%; τ stands for the shear yield stress, Pa; m and n represent the fitting parameters.

382

383

384

$$U_{\text{Flocculant condition}} = a \cdot c^b \quad (2)$$

385

Where c stands for the compressive yield stress, kPa; a and b represent the fitting parameters.

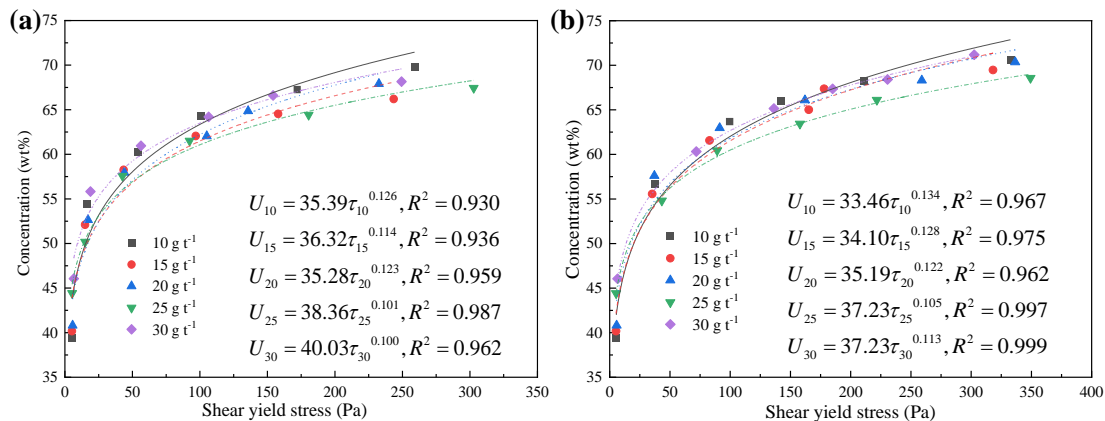
386

387

Figures 8(a) and 8(b) show the fitting results of concentration-shear yield stress under compression effect and compression-shear coupling effect with different

388

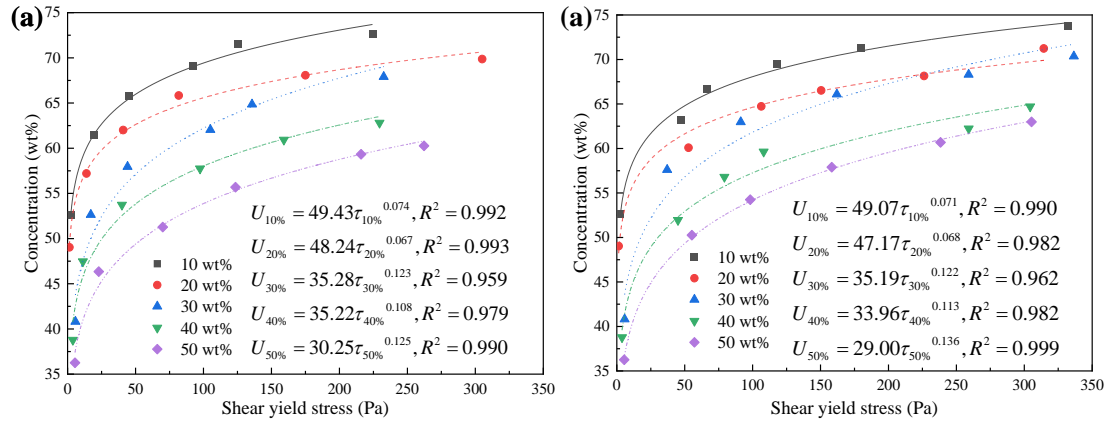
389 flocculant dosages. The relationship between concentration and shear yield
 390 stress conforms to a power function. The R^2 values corresponding to each
 391 flocculant dosage level under the compression effect are 0.930, 0.936, 0.959,
 392 0.987, and 0.962, respectively. The R^2 values under the compression-shear
 393 coupling effect are 0.967, 0.975, 0.962, 0.997, and 0.999, respectively,
 394 indicating that the fitting results are reliable.



395

396 Fig. 8 Fitting results of concentration-shear yield stress under different flocculant dosages: (a)
 397 Compression effect; (b) Compression-shear coupling effect

398 Figures 9(a) and 9(b) show the fitting results of concentration-shear yield stress
 399 under the compression and compression-shear coupling effects with different
 400 fine-grained tailings contents. With the growth of fine-grained tailings content,
 401 the overall concentration curves decrease continuously, indicating that high
 402 fine-grained tailings content has an adverse effect on the concentration. The
 403 relationship between concentration and shear yield stress under compression
 404 effect and compression-shear coupling effect is a power function. The fitted R^2
 405 values under the compression effect are 0.992, 0.993, 0.959, 0.979, and 0.990,
 406 respectively, and the fitted R^2 values under the compression-shear coupling
 407 effect are 0.990, 0.982, 0.962, and 0.990, respectively. Moreover, the fitting
 408 coefficient m of the Eq. (1) under the compression and compression-shear
 409 coupling effects decreases with the increase of fine-grained tailings content.
 410 The larger the fitting parameter m is, the better the thickening effect is, and the
 411 higher the concentration is. Hence, the concentration fitting curve shown in
 412 Figures 9(a) and 9(b) decreases with the increase of fine-grained tailings
 413 content.



414

415

416

417

Fig. 9 Fitting results of concentration-shear yield stress under different fine-grained tailings contents: (a) Compression effect; (b) Compression-shear coupling effect

3.2.2 Concentration-compressive yield stress

418

419

420

421

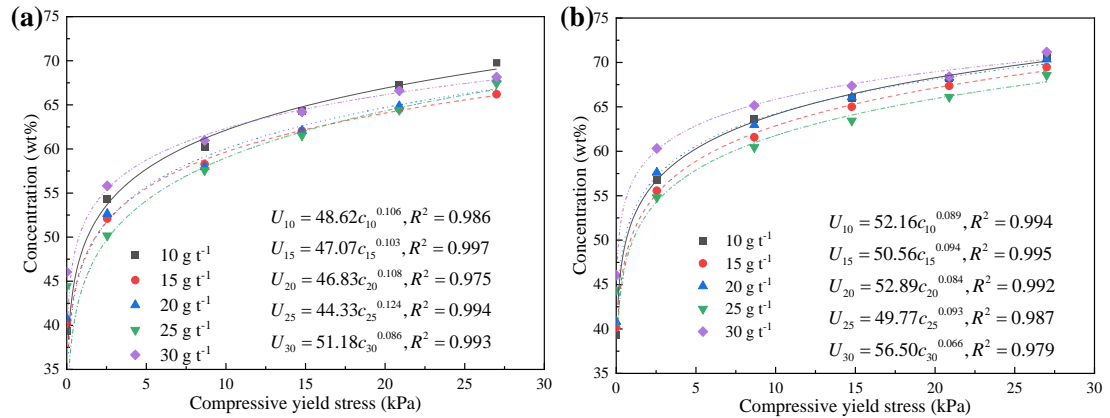
422

423

424

425

Figures 10(a) and 10(b) show the fitting results of concentration-compressive yield stress under the compression and compression-shear coupling effects with different flocculant dosages. It can be seen from the figure that the relationship between concentration and compressive yield stress is a power function. The fitted R^2 values under the compression effect are 0.986, 0.997, 0.975, 0.994, and 0.993, respectively, and the fitted R^2 values under the compression-shear coupling effect are 0.994, 0.995, 0.992, 0.987, and 0.979, respectively.



426

427

428

Fig. 10 Fitting results of concentration-compressive yield stress under different flocculant dosages: (a) Compression effect; (b) Compression-shear coupling effect

429

430

431

432

433

434

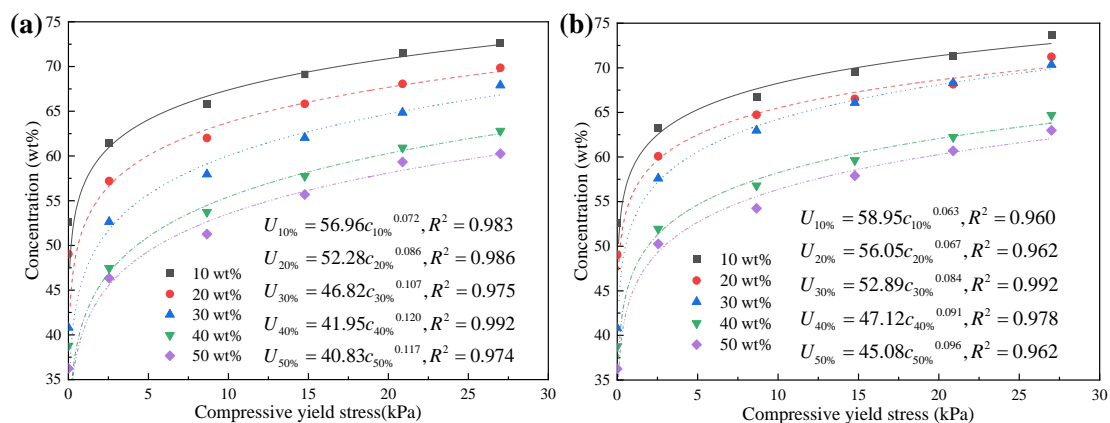
435

436

437

Figures 11(a) and 11(b) show the fitting results of concentration-compressive yield stress under the compression and compression-shear coupling effects with different fine-grained tailings contents. With the increase of fine-grained tailings content, the overall concentration curves move down continuously, indicating that high fine-grained tailings content has an adverse effect on the concentration. There is a power function relationship between concentration and compressive yield stress. The fitted R^2 values under the compression effect are 0.983, 0.986, 0.975, 0.992, and 0.974, respectively, and the fitted R^2 values under the compression-shear coupling effect are 0.960, 0.962, 0.992, and

438 0.974, respectively. Among them, the coefficient a of the fitting Eq. (2) under
 439 the compression and compression-shear coupling effects decreases with the
 440 increase of fine-grained tailings content, which shows again that the fine-
 441 grained tailings content has an adverse influence on the thickening effect, and
 442 the larger the fitting parameters a is, the better the thickening effect is and the
 443 higher the concentration is. Therefore, the concentration curve shown in
 444 Figures 11(a) and (b) decreases with the increase of fine-grained tailings
 445 content.



446

447 Fig. 11 Fitting results of concentration-compressive yield stress under different fine-grained
 448 tailings contents: (a) Compression effect; (b) Compression-shear coupling effect

449 3.2.3 Shear yield stress-compressive yield stress

450 A lot of research has been carried out to analyze the relationship between shear
 451 yield stress and compressive yield stress. Still, most of the research on
 452 thickened tailings is carried out under low compression stress (< 1 kPa), which
 453 is quite different from the high compression stress in industrial thickeners
 454 [23,29]. Therefore, studying the high compression stress of 0-30 kPa in this
 455 study is of great practical value. From the analysis in Section 3.1, it can be seen
 456 that there is a linear correlation between the shear yield stress and the
 457 compressive yield stress. Linear fitting (Eq. (3)) of shear yield stress-
 458 compressive yield stress under the compression and compression-shear
 459 coupling effects was carried out, respectively.

460

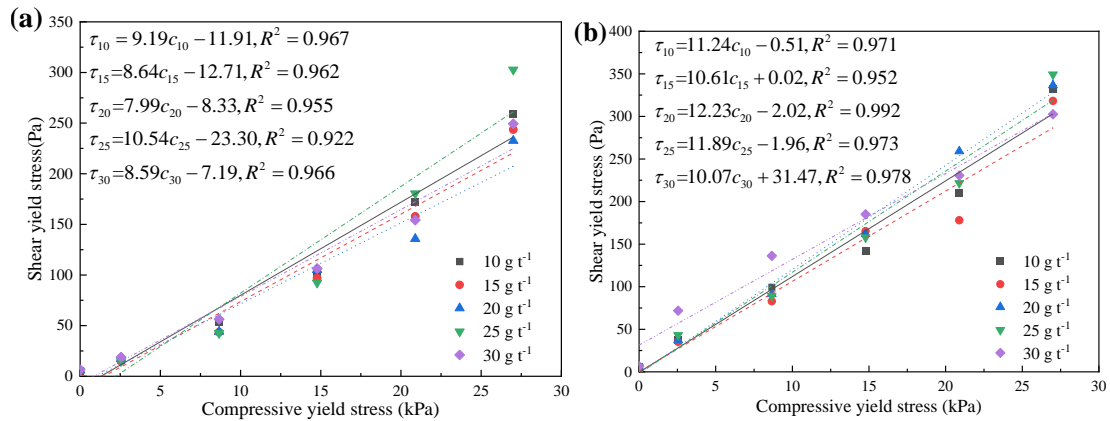
$$\tau = kc + p \quad (3)$$

461 Where k and p are the fitting parameters.

462 Fig. 12 shows the linear fitting results of shear yield stress-compressive yield
 463 stress under the compression and compression-shear coupling effects with
 464 different flocculant dosages. As shown in Fig. 12(a), the linear fitting R^2 values
 465 of different flocculant dosage levels under the compression effect are 0.967,
 466 0.962, 0.955, 0.922, and 0.966, respectively. As shown in Fig. 12(b), under the
 467 compression-shear coupling effect, the linear fitting R^2 values of different
 468 flocculant dosages are 0.971, 0.952, 0.992, 0.973, and 0.978, respectively. The
 469 fitting effects are reliable.

470 A comparative analysis was conducted on the proportion coefficients (fitting line

471 slope k) of the fitting lines between shear yield stress and compressive yield stress under compression effect and compression-shear coupling effect, where
 472 stress under compression effect and compression-shear coupling effect, where
 473 the proportion coefficient represents the thickening rate of the thickened tailings.
 474 As shown in Fig. 13, the proportional coefficients of each flocculant dosage level
 475 under the compression effect are smaller than those under the compression-
 476 shear coupling effect, indicating that the thickening rate under compression-
 477 shear coupling effect is faster and the thickening effect is better, which is
 478 consistent with the fact that the concentration under compression-shear
 479 coupling effect is higher than that under compression effect.

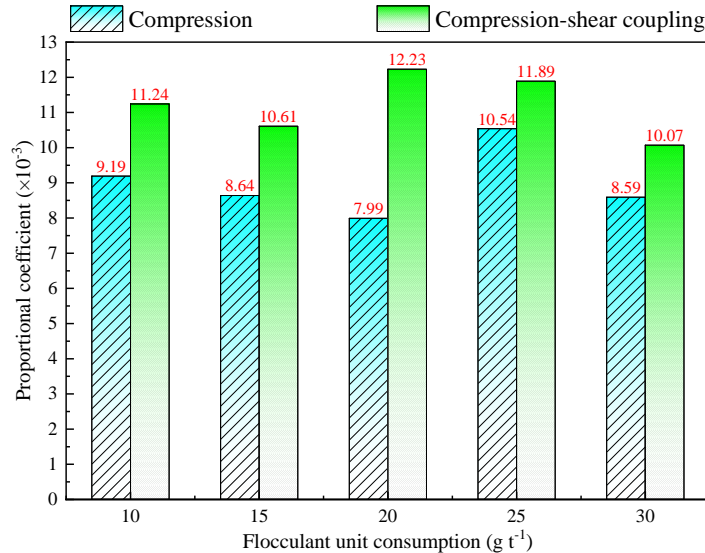


480

481

482

Fig. 12 Fitting results of shear yield stress-compressive yield stress with different flocculant dosages: (a) Compression; (b) Compression-shear coupling



483

484

485

486

Fig. 13 Comparative analysis of the proportional coefficients of the shear yield stress-compressive yield stress fitting lines under compression and compression-shear coupling effects with different flocculant dosages

487

488

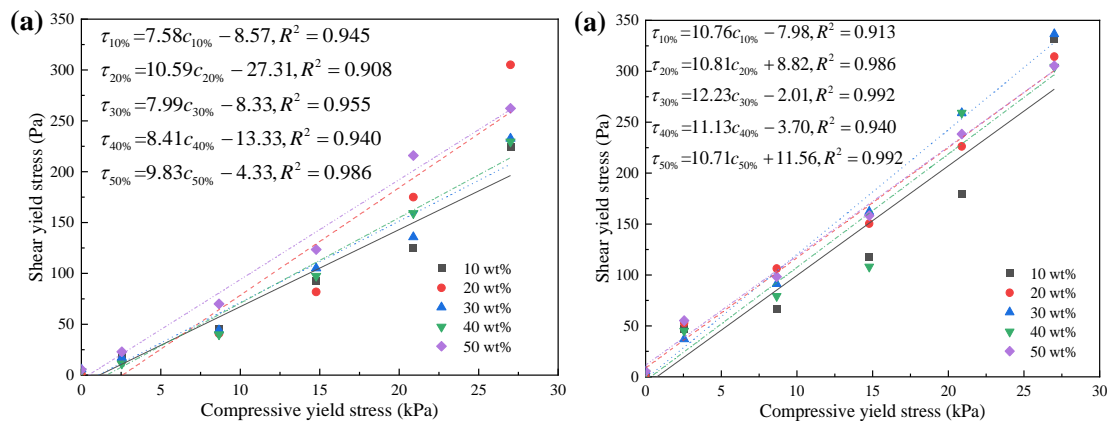
489

490

491

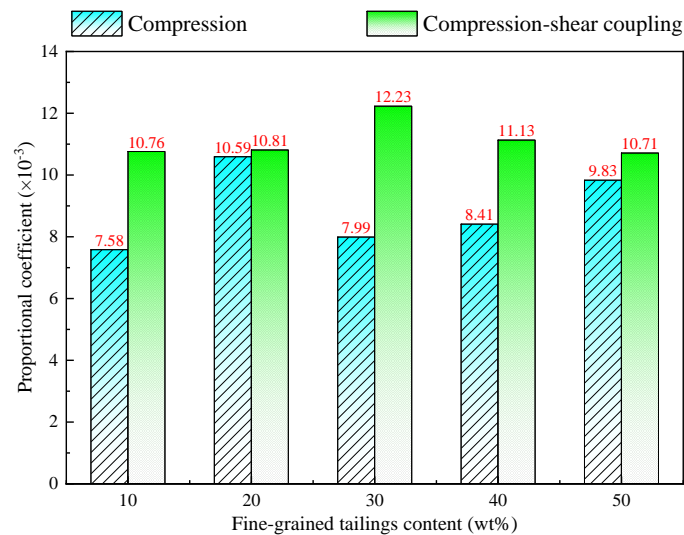
Fig. 14 shows the linear fitting results of shear yield stress-compressive yield stress under the compression and compression-shear coupling effects with different fine-grained tailings contents. As shown in Fig. 14(a), the linear fitting R^2 values of different fine-grained tailings contents under the compression effect are 0.945, 0.908, 0.955, 0.940, and 0.986, respectively. As shown in Fig.

492 14(b), under the compression-shear coupling effect, the linear fitting R^2 values
 493 of different fine-grained tailings contents are 0.913, 0.986, 0.992, 0.940, and
 494 0.992, respectively, and the fitting effects are reliable. The proportional
 495 coefficients of shear yield stress-compressive yield stress fitting lines under
 496 compression and compression-shear coupling effects were compared and
 497 analyzed in Fig. 15. The proportional coefficients of each fine-grained tailings
 498 content level under compression effect are all lower than those under
 499 compression-shear coupling effect, which once again shows that the thickening
 500 rate is faster and the thickening effect is better, and it is also verified that the
 501 concentration under compression-shear coupling effect is higher than that
 502 under compression effect.



503
 504
 505

Fig. 14 Fitting results of shear yield stress-compressive yield stress with different fine-grained tailings contents: (a) Compression effect; (b) Compression-shear coupling effect



506
 507
 508
 509

Fig. 15 Comparative analysis of the proportional coefficients of the shear yield stress-compressive yield stress fitting lines under compression and compression-shear coupling effects with different fine-grained tailings contents

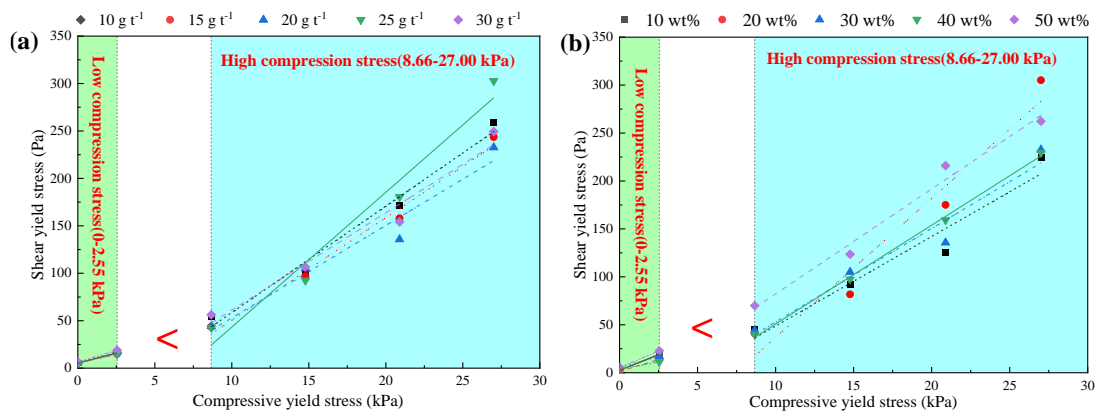
510 3.3 Thickening mechanism

511 In this study, the compressive yield stress range of the experiment is divided
 512 into two stages, namely, low compression stress range and high compression
 513 stress range. Among them, the low compression stress range is 0-2.55 kPa,

514 and the high compression stress range is 8.66-27 kPa. The low compression
 515 stress range is consistent with the compression stress range of the indoor
 516 thickening experiments, and the high compression stress range is consistent
 517 with the high mud layer pressure in the industrial thickeners. The evolution of
 518 shear yield stress and compressive yield stress in low and high compression
 519 stress ranges under the compression and compression-shear coupling effects
 520 with different flocculant dosages and fine-grained tailings contents were fitted,
 521 respectively. The corresponding proportional coefficients of low and high
 522 compression stress ranges are obtained and compared to reveal the thickening
 523 mechanism.

524 3.3.1 Thickening mechanism under compression

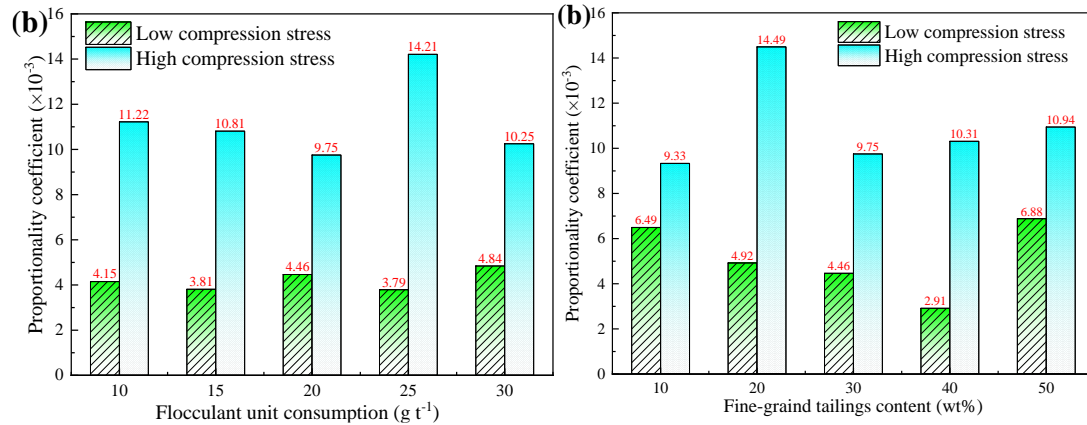
525 As shown in Figures 16(a) and 16(b), they are the fitting results of low and high
 526 compression stress ranges under the compression effect with different
 527 flocculant dosages and fine-grained tailings contents. It can be seen that the
 528 slopes of the fitting straight lines in the low compression stress range are lower
 529 than that in the high compression stress range, indicating that under
 530 compression effect, the thickening rate in the low compression stress range is
 531 lower than that in the high compression stress range.



532

533 Fig. 16 Comparison of proportional coefficients between low and high compression stress
 534 ranges under compression effect: (a) Flocculant dosage; (b) Fine-grained tailings content.

535 From the comparative analysis of the proportional coefficients of the low and
 536 the high compression stress ranges shown in Figures 17(a) and 17(b), it can
 537 also be seen that the proportional coefficients of the high compression stress
 538 range corresponding to different flocculant dosages and fine-grained tailings
 539 contents are higher than those in the low compression stress range.



540

541

542

543

544

545

546

547

548

549

550

551

552

553

554

555

556

557

558

559

560

561

562

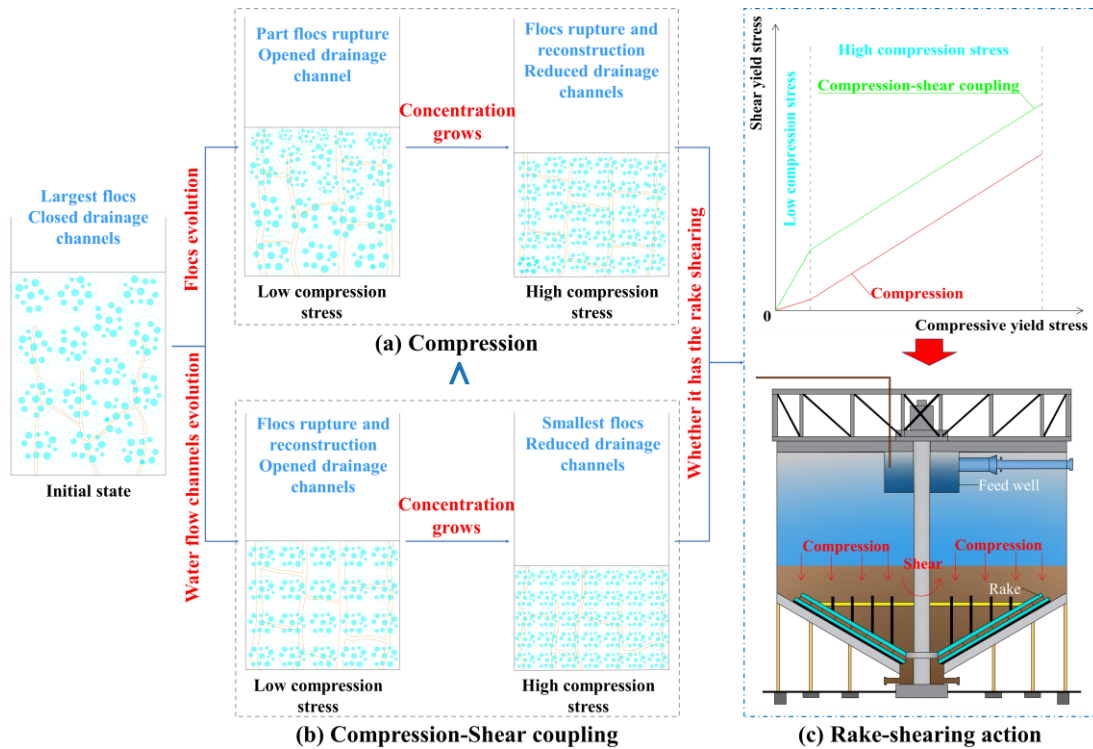
563

564

Fig. 17 Comparison of k values between low and high compression stress ranges under compression effect: (a) Flocculant dosage; (b) Fine-grained tailings content

The thickening process of thickened tailings is accompanied by the evolution of flocs structure and the drainage channels, which is the important internal mechanism causing the evolution of double yield stress [43,48]. The evolution of flocs mainly manifests as their rupture and reconstruction, releasing the stored water in the flocs [43]. The evolution of drainage channels is mainly through increasing the connectivity of channels. The water between flocs is discharged to the solid-liquid separation interface [49-51].

As shown in Fig. 18, in the initial state of the thickened tailings, the tailings floc size is the largest, the floc arrangement is disordered, the drainage channels are in low quantity, the connectivity is low, most of the channels are blocked, and there is a large amount of water between and inside the flocs, the concentration and shear yield stress are low. Under the low compression stress range (Fig. 18(a)), the tailings flocs partially rupture and reconstruct at the top of the thickened tailings. However, most of the flocs remain in the original state at the bottom of the thickened tailings. Because there is a large amount of water between and inside the flocs, the shear resistance is weak, and the shear yield stress increases slowly. Under the high compression stress range, flocs undergo large-scale rupture and reconstruction, and flocs are in a disordered arrangement, drainage channels decrease, channels close, connectivity decreases, thickening effect is poor, and the shear resistance of thickened tailings is enhanced due to the decrease of water content between and inside flocs. Moreover, the growth rate of shear yield stress increases (Fig. 18(c)).

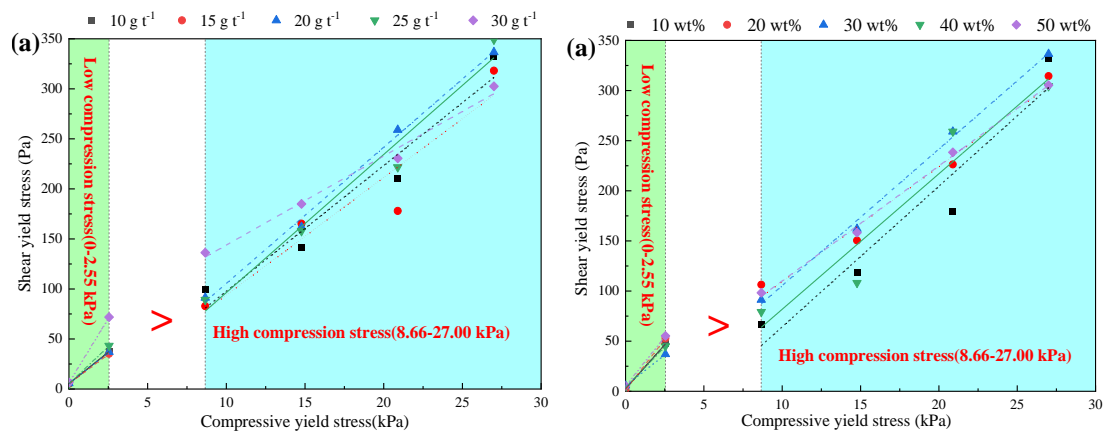


565
566
567
568
569
570
571
572
573
574
575
576
577

Fig. 18 Influence of floc structure and drainage channel evolutions on thickening process

3.3.2 Thickening mechanism under compression-shear coupling

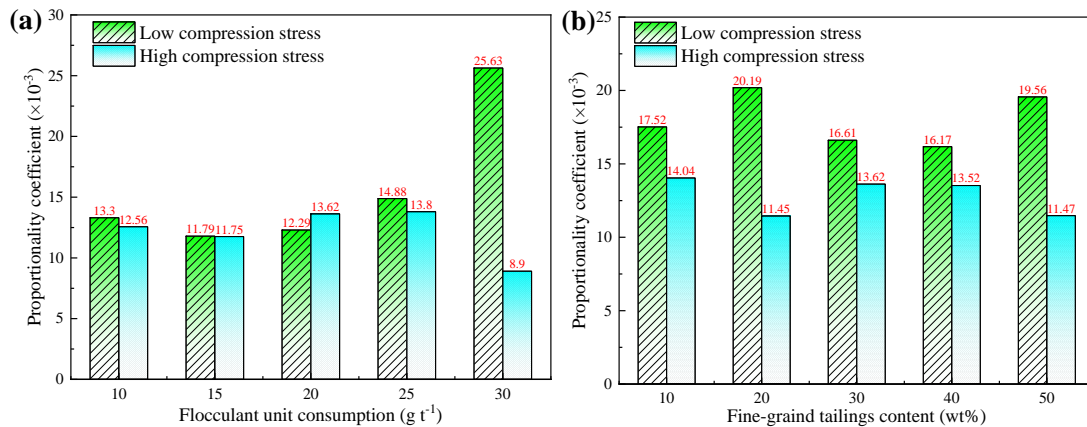
As shown in Figures 19(a) and 19(b), they are the fitting results of low and high compression stress ranges under the compression-shear coupling effect under different flocculant dosages and fine-grained tailings contents. It can be seen that the slopes of the fitting straight lines in the low compression stress range are obviously higher than that in the high compression stress range, indicating that under the compression-shear coupling effect, the thickening rate in the low compression stress range is higher than that in the high compression stress range, thereby improving the overall thickening effect. This also confirms that the thickening effect of the compression shear coupling effect is better than that of the compression effect.



578
579
580
581

Fig. 19 Comparison of proportional coefficients between low and high compression stress ranges under compression-shear coupling effect: (a) Flocculant dosage; (b) Fine-grained tailings content

582 From the comparative analysis of the proportional coefficients of the low and
 583 the high compression stress ranges shown in Figures 20(a) and 20(b), it can
 584 also be seen that the proportional coefficients of the high compression stress
 585 range corresponding to different flocculant dosages and fine-grained tailings
 586 contents are mostly lower than those in the low compression stress range. It
 587 shows that the thickening rate in the low compression stress range is higher
 588 than that in the high compression stress range. Moreover, the proportion
 589 coefficients in the low compression stress range under the compression-shear
 590 coupling effect are much higher than those under the compression effect, and
 591 the proportion coefficients in the high compression stress range are roughly
 592 similar in both thickening conditions. Corresponding to the proportional
 593 coefficients of shear yield stress-compressive yield stress under the
 594 compression-shear coupling effect (Fig. 12 and Fig. 14), it also shows that the
 595 thickening rate under the compression-shear coupling effect is higher, which
 596 verifies the conclusion that the concentration under compression-shear
 597 coupling effect is higher than that under compression effect.



598

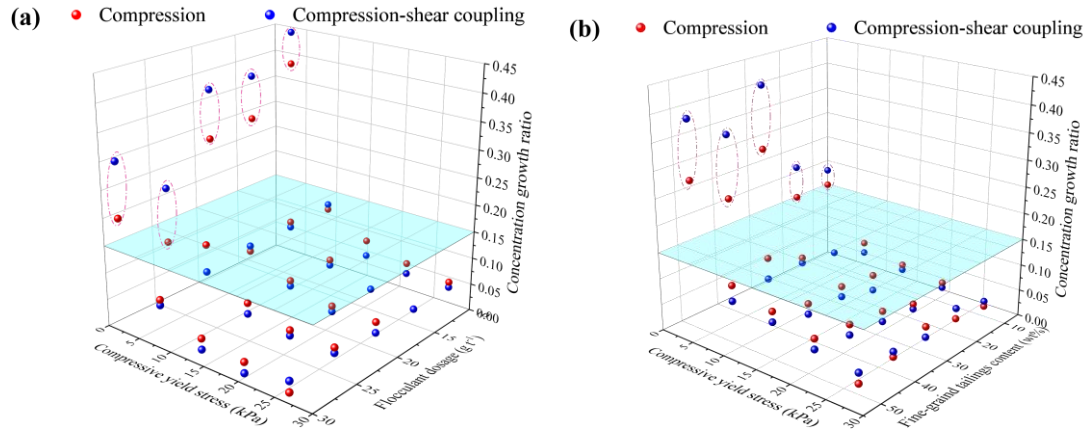
599 Fig. 20 Comparison of k values between low and high compression stress ranges under
 600 compression-shear coupling effect: (a) Flocculant dosage; (b) Fine-grained tailings content
 601 As shown in Fig. 18(b), under the compression-shear coupling effect, many
 602 flocs break under the lower compression stress acts on the thickened tailings.
 603 The rake-shearing action will cause flocs to rearrange. Meanwhile, it also
 604 promotes the opening of the drainage channels. The channel size is large, the
 605 connectivity is high, the thickening effect is good, the flocs structure is compact,
 606 and the water between and inside the flocs is discharged with the drainage
 607 channels. Compared with the compression effect, the concentration increases
 608 more rapidly. Due to the large amount of water discharged between and inside
 609 the flocs, the shear resistance is enhanced, and the shear yield stress also
 610 increases fast. In the higher compression stress range, the tailings floc ruptures
 611 and restructures under rake-shearing and finally forms the smallest floc size
 612 and the largest floc quantity. Due to the further discharge of water between flocs,
 613 the structure is compact, the quantity of the drainage channels reduces, the
 614 connectivity decreases, the thickening rate decreases. Furthermore, the shear
 615 resistance changes little, and the shear yield stress increases at a lower rate

616 (Fig. 18(c)) compared to the low compression stress range.

617 **3.3.3 Comparison of thickening mechanisms between compression and** 618 **compression-shear coupling effects**

619 According to the comparative analysis of the proportional coefficients of shear
620 yield stress-compressive yield stress in the low and high compression stress
621 ranges in Sections 3.3.1 and 3.3.2, it can be seen that compared with the
622 compression effect, the compression-shear coupling effect greatly improves the
623 thickening rate and thickening effect in the low compression stress range by
624 introducing the rake-shearing action. The concentration growth ratio varies with
625 different compression stresses. Therefore, the growth ratios of concentration
626 corresponding to different compression stresses are also an important factor to
627 measure the thickening mechanism. The thickening mechanism was further
628 verified by the growth ratio of concentration. The growth ratios of concentration
629 with different compressive yield stresses under compression and compression-
630 shear coupling effects with varying flocculant dosages of and fine-grained
631 tailings contents were analyzed, respectively.

632 According to the growth ratios of concentration, the three-dimensional
633 distribution diagrams of concentration growth ratio are shown in Figures 21(a)
634 and 21(b). Under the high compressive yield stress of 8.66, 14.78, 20.89, and
635 27.00 kPa, there is no significant difference in the growth ratio of concentration,
636 which is all less than 0.15. The main difference occurs at a low compressive
637 yield stress of 2.55 kPa. As can be seen from Fig. 21, there is a large difference
638 between the growth ratio of concentration under the compression-shear
639 coupling effect and compression effect corresponding to 2.55 kPa, and the
640 growth ratios of concentration under compression-shear coupling effect are
641 significantly higher than that under the compression effect. It is verified that the
642 thickening rate and effect in the low compression stress range are greatly
643 improved by the introduction of rake-shearing action under the compression-
644 shear coupling effect, and the thickening mechanism that the concentration
645 under the compression-shear coupling effect is higher than that under the
646 compression effect is also revealed (Fig. 18(c)). Therefore, it is suggested to
647 adopt the deep-cone structure with high mud layer pressure and the rake-
648 shearing structure for industrial thickeners.



649

650 Fig. 21 Distribution diagram of concentration growth ratio under compression effect and
 651 compression-shear coupling effect: (a) Flocculant dosage; (b) Fine-grained tailings content

652 **4 Conclusion**

653 In this study, the rheological properties and concentration of thickened tailings
 654 under compression and compressed-shear coupling effects were tested with
 655 different flocculant dosages and fine-grained tailings contents. Concentration-
 656 double yield stress correlation analysis, and thickening mechanism analysis
 657 were carried out. The main conclusions are as follows:

658 (1) The concentration increases rapidly in the low compression stress range
 659 and slowly in the high compression stress range with the linear growth of
 660 compressive yield stress and shear yield stress, and the concentration under
 661 the compression-shear coupling effect is higher than that under the
 662 compression effect. The higher the fine-grained tailings content, the lower the
 663 concentration. The shear yield stress increases linearly with the growth of
 664 compressive yield stress.

665 (2) There is a power function relationship between concentration and shear
 666 yield stress and compressive yield stress, respectively. The fitting curves under
 667 different fine-grained tailings contents move down with the increase of fine-
 668 grained tailings content.

669 (3) The linear fitting of the relationship under each experimental factor shows
 670 that the proportional coefficients under the compression effect are smaller than
 671 that under the compression-shear coupling effect, indicating that the thickening
 672 rate is higher and the thickening effect is better under the compressor-shear
 673 coupling effect.

674 (4) The thickening mechanism was analyzed from the perspective of the double
 675 yield stress relationship and evolution of flocs and drainage channels. The
 676 thickening rate in the low compression stress range under compression is
 677 higher than that in the high compression stress range, but under the
 678 compression-shear coupling effect, this phenomenon is the opposite.

679 (5) The concentration growth ratio shows that the difference of concentration
 680 growth ratio between the compression effect and compressor-shear coupling
 681 effect is mainly concentrated in the low compression stress range of 0-2.55kPa,
 682 indicating that compared with a compression effect, the introduction of rake-

683 shearing action under compression-shear coupling effect mainly increases the
684 thickening rate in the low compression stress range, and then increases the
685 overall thickening effect, revealing the thickening mechanism with higher
686 concentration under the compression-shear coupling effect.

687 **Acknowledgment**

688 This work was funded by the National Natural Science Foundation of China (no.
689 52130404, 52304121), the Fundamental Research Funds for the Central
690 Universities (no.FRF-TP-22-112A1), Guangdong Basic and Applied Basic
691 Research Foundation (no. 2021A1515110161), ANID (Chile) through Fondecyt
692 project 1210610, Centro de Modelamiento Matemático (BASAL funds for
693 Centers of Excellence FB210005), CRHIAM project ANID/FONDAP/15130015,
694 and Anillo project ANID/ACT210030.

695 **Conflict of Interest**

696 The authors declare no conflict of interest.

697 **References**

- 698 [1] Menglong Wu, Yicheng Ye, Nanyan Hu, Qihu Wang, Wenkan Tan.
699 Scientometric analysis on the review research evolution of tailings dam failure
700 disasters. *Environmental Science and Pollution Research*. 2023, 30: 13945–
701 13959.
- 702 [2] Yong Wang, Zhenqi Wang, Aixiang Wu, Liang Wang, Qing Na, Chen Cao,
703 Gangfeng Yang. Experimental research and numerical simulation of the multi-
704 field performance of cemented paste backfill: Review and future perspectives.
705 *International Journal of Minerals Metallurgy and Materials*. 2023, 30(2):193-208.
- 706 [3] Dylan D. Furszyfer Del Rio, Benjamin K. Sovacool, Aoife M. Foley, Steve
707 Griffiths, Morgan Bazilian, Jinsoo Kim, David Rooney. Decarbonizing the glass
708 industry: A critical and systematic review of developments, sociotechnical
709 systems and policy options. *Renewable and Sustainable Energy Reviews*. 2022,
710 155.
- 711 [4] Mansour Edraki, Thomas Baumgartl, Emmanuel Manlapig, Dee
712 Bradshaw, Daniel M. Franks, Chris J. Moran. Designing mine tailings for better
713 environmental, social and economic outcomes: a review of alternative
714 approaches. *Journal of Cleaner Production*. 2014, 84: 411-420.
- 715 [5] You Zheng, Jianzhong Xiao, Jinhua Cheng. Industrial Structure
716 Adjustment and Regional Green Development from the Perspective of Mineral
717 Resource Security. *International Journal of Environmental Research and Public
718 Health*. 2020, 17(19).
- 719 [6] Aixiang Wu, Zhuen Ruan, Jiandong Wang, Rheological behavior of paste
720 in metal mines, *Int J Miner Metall Mater*, 2022, 29: 717–726.
- 721 [7] Chongchong Qi, Andy Fourie. Cemented paste backfill for mineral tailings
722 management: Review and future perspectives. *Minerals Engineering*. 2019,
723 144.
- 724 [8] Zhenqi Wang, Yong Wang, Liang Cui, Cheng Bi, Aixiang Wu. Insight into
725 the isothermal multiphysics processes in cemented paste backfill: Effect of
726 curing time and cement-to-tailings ratio. *Construction and Building Materials*.

727 2022, 235.

728 [9] Shan Gao, Wei Li, Kekuo Yuan, Chuanxin Rong. Properties and
729 application of thixotropic cement paste backfill with molybdenum tailings.
730 Journal of Cleaner Production. 2023, 391.

731 [10] Xiaoyan Zhang, Muyan Xu, Lang Liu, Chao Huan, Yujiao Zhao, Chongc
732 hong Qi, KI-IL Song. Experimental study on thermal and mechanical properties
733 of cemented paste backfill with phase change material. Journal of Materials
734 Research and Technology. 2020, 9(2): 2164-2175.

735 [11] Huazhe Jiao, Shufei Wang, Yixuan Yang, Xinming Chen. Water recovery
736 improvement by shearing of gravity-thickened tailings for cemented paste
737 backfill. Journal of Cleaner Production. 2020, 245.

738 [12] Lihua Yang, Jincang Li, Hongbin Liu, Huazhe Jiao, Shenghua Yin,
739 Xinming Chen, Yang Yu. Systematic review of mixing technology for recycling
740 waste tailings as cemented paste backfill in mines in China. International
741 Journal of Minerals Metallurgy and Materials. 2023, 30: 1430–1443.

742 [13] Haiyong Cheng, Shunchuan Wu, Hong Li, Xiaoqiang Zhang. Influence of
743 time and temperature on rheology and flow performance of cemented paste
744 backfill. Construction and Building Materials. 2020, 231.

745 [14] Lang Liu, Chao Zhu, Chongchong Qi, Mei Wang, Chao Huan, Bo Zhang,
746 KI-IL Song. Effects of curing time and ice-to-water ratio on performance of
747 cemented paste backfill containing ice slag. Construction and Building Materials,
748 2019, 228.

749 [15] Coe H S, Clevenger G H. Methods for determining the capacity of slime
750 settling tanks. Traps. A1ME. 1916, 55: 356-385.

751 [16] Kynch G J. A theory of sedimentation. Traps Faraday Soc. 1952, 48(2):
752 166-176.

753 [17] Liyi Zhu, Wensheng Lyu, Peng Yang, Zhikai Wan. Effect of ultrasound on
754 the flocculation-sedimentation and thickening of unclassified tailings.
755 Ultrasonics Sonochemistry. 2020, 66.

756 [18] Qiuyi Lu, Bin Yan, Lei Xie, Jun Huang, Yang Liu, Hongbo Zeng. A two-
757 step flocculation process on oil sands tailings treatment using oppositely
758 charged polymer flocculants. Science of The Total Environment. 2016, 565:
759 369-375.

760 [19] Lianfu Zhang, Hongjiang Wang, Aixiang Wu, Bern Klein. Predicting beach
761 profiles for thickened tailings surface deposition. Minerals Engineering.
762 2023, 201.

763 [20] R. Arjmand, M. Massinaei, A. Behnamfard. Improving flocculation and
764 dewatering performance of iron tailings thickeners. Journal of Water Process
765 Engineering. 2019, 31.

766 [21] Weicheng Ren, Rugao Gao, Youzhi Zhang, Maoxin Hou. Rheological
767 Properties of Ultra-Fine Tailings Cemented Paste Backfill under Ultrasonic
768 Wave Action. Minerals. 2021, 11(7).

769 [22] Claudia Castillo, Christian F. Ihle, Ricardo I. Jeldres. Chemometric

770 Optimisation of a Copper Sulphide Tailings Flocculation Process in the
771 Presence of Clays. *Minerals*. 2019, 9(10).

772 [23] Xuetao Wang, Baoyu Cui, Dezhou Wei, Zhenguo Song, Yi He, Andrew E.
773 Bayly. CFD-PBM modelling of tailings flocculation in a lab-scale gravity
774 thickener. *Powder Technology*. 2022, 396: 139-151.

775 [24] Mohammed Derqaoui, Imane Aarab, Abdelmoughit Abidi, Abdelrani
776 Yaacoubi, Khalid El Amari, Abderahman Etahiri, Abdelaziz Baçaoui. The effect
777 of calcium ions on the flotation behavior of fluorapatite. *Mineral Processing and*
778 *Extractive Metallurgy Review*. 2022, 1-10.

779 [25] Juan I. Langlois, Aldo Cipriano. Dynamic modeling and simulation of
780 tailing thickener units for the development of control strategies. *Minerals*
781 *Engineering*. 2019, 131: 131-139.

782 [26] Chenyu Fang, Dakuo He, Kang Li, Yan Liu, Fuli Wang. Image-based
783 thickener mud layer height prediction with attention mechanism-based CNN.
784 *ISA Transactions*. 2022, 128: 677-689

785 [27] . Rudman, K. Simic, D.A. Paterson, P. Strode, A. Brent, I.D. Šutalo. Raking
786 in gravity thickeners. *International Journal of Mineral Processing*. 2008, 86: 114-
787 130.

788 [28] M. Rudman, D.A. Paterson, K. Simic. Efficiency of raking in gravity
789 thickeners. *International Journal of Mineral Processing*. 2010, 95: 30-39.

790 [29] J.B Farrow, R.R.M Johnston, K Simic, J.D Swift. Consolidation and
791 aggregate densification during gravity thickening. *Chemical Engineering*
792 *Journal*. 2000, 80: 141-148.

793 [30] Jinglong Gao, Andy Fourie. Using the flume test for yield stress
794 measurement of thickened tailings. *Minerals Engineering*. 2015, 81:116-127.

795 [31] S KY Gawu and A B Fourie. Assessment of the modified slump test as a
796 measure of the yield stress of high-density thickened tailings. *Canadian*
797 *Geotechnical Journal*. 2011, 41(1): 39-47.

798 [32] Shabnam Mizani, Paul Simms. Method-dependent variation of yield
799 stress in a thickened gold tailings explained using a structure based viscosity
800 model. *Minerals Engineering*. 2016, 98: 40-48.

801 [33] Yong Wang, Aixiang Wu, Zhuen Ruan, Zihui Wang, Zongsu Wei,
802 Gangfeng Yang, Yiming Wang. Reconstructed rheometer for direct monitoring
803 of dewatering performance and torque in tailings thickening process.
804 *International Journal of Minerals Metallurgy and Materials*. 2020, 27: 1430–
805 1437.

806 [34] Zhuen Ruan, Aixiang Wu, Raimund Bürger, Fernando Betancourt, Yiming
807 Wang, Yong Wang, Huazhe Jiao, Shengkai Wang. Effect of interparticle
808 interactions on the yield stress of thickened flocculated copper mineral tailings
809 slurry. *Powder Technology*. 2021, 392: 278-285.

810 [35] David V. Boger. Rheology and the resource industries. *Chemical*
811 *Engineering Science*. 2009, 64(22): 4525-4536.

812 [36] K. El Mahboub, M. Mbonimpa, T. Belem, A. Maqsoud. Rheological

813 characterization of cemented paste backfills containing superabsorbent
814 polymers (SAPs). *Construction and Building Materials*. 2022, 317.

815 [37] Matías. Jeldres, Norman Toro, Sandra Gallegos, Pedro Robles, Iván
816 Salazar, Phillip D. Fawell, Ricardo I. Jeldres. Reducing Magnesium within
817 Seawater Used in Mineral Processing to Improve Water Recovery and
818 Rheological Properties When Dewatering Clay-Based Tailings. *Polymers*. 2022,
819 14(2).

820 [38] Rachel Bryan, Paul Simms, Rens Verburg. Coupling oxidation to transient
821 drying during multilayer deposition of thickened gold tailings. *Minerals*
822 *Engineering*. 2010, 23(14): 1101-1112.

823 [39] Shi Wang, Xuepeng Song, Xiaojun Wang, Qiusong Chen, Jianchun Qin,
824 Yuxian Ke. Influence of coarse tailings on flocculation settlement. *International*
825 *Journal of Minerals Metallurgy and Materials*. 2020,27: 1065–1074.

826 [40] Shenghua Yin, Yongqiang Hou, Shixing Yang, Xin Chen. Study on static
827 and dynamic flocculation settlement characteristics of fine tailings slurry and
828 influence of flocculant on strength of fine tailings backfill. *Case Studies in*
829 *Construction Materials*. 2022, 17.

830 [41] Mehdi Rahimi, Ali A. Abdollahzadeh, Bahram Rezai. Dynamic simulation
831 of tailing thickener at the Tabas coal washing plant using the phenomenological
832 model. *International Journal of Mineral Processing*. 2016, 154: 35-40.

833 [42] Michael R. MacIver, Marek Pawlik. A floc structure perspective on
834 sediment consolidation in thickened tailings. *Chemical Engineering Science*.
835 2202, 263.

836 [43] Philip Ofori, Anh V. Nguyen, Bruce Firth, Clint McNally, Orhan Ozdemir.
837 Shear-induced floc structure changes for enhanced dewatering of coal
838 preparation plant tailings. *Chemical Engineering Journal*. 2011, 172: 914-923.

839 [44] Dan Zhang, Tinu Abraham, Trong Dang-Vu, Jonathan Xu, Sarang P.
840 Gumfekar, Thomas Thundat. Optimal floc structure for effective dewatering of
841 polymer treated oil sands tailings. *Minerals Engineering*. 2021,160.

842 [45] Di Zheng, Weidong Song, Yuye Tan, Shuai Cao, Zilong Yang, Lijuan Sun.
843 Fractal and microscopic quantitative characterization of unclassified tailings
844 flocs. *International Journal of Minerals Metallurgy and Materials*. 2021, 28:
845 1429–1439.

846 [46] Huazhe Jiao, Wenbo Yang, Zhu'en Ruan, Jianxin Yu, Juanhong Liu,
847 Yixuan Yang. Microscale mechanism of tailing thickening in metal mines.
848 *International Journal of Minerals Metallurgy and Materials*. 2023, 30: 1538–154.

849 [47] Vold M J. Computer simulation of floc formation in a colloidal suspension.
850 *Journal of Colloid Science*. 1963, 7: 684-695.

851 [48] Huazhe Jiao, Wenxiang Zhang, Yixuan Yang, Lihua Yang, Kaijian Hu,
852 Jianxin Yu. Pore Structure Evolution and Seepage Characteristics in
853 Unclassified Tailing Thickening Process. *Minerals*. 2022, 12(2).

854 [49] Gezhong Chen, Cuiping Li, Zhuen Ruan, Raimund Bürger, Yuan Gao, Hezi
855 Hou, Structural evolution of bed drainage channels under the shear effect

856 of the whole process of tailings thickening, Minerals Engineering, 2023, 203.
857 [50] Xinming Chen, Xiangfei Jin, Huazhe Jiao, Yixuan Yang, Juanhong Liu.
858 Pore Connectivity and Dewatering Mechanism of Tailings Bed in Raking Deep-
859 Cone Thickener Process. Minerals. 2020, 10(4).
860 [51]Gezhong Chen, Cuiping Li, Zhuen Ruan, Raimund Bürger, Hezi Hou,
861 Research on floc structure and physical properties based on pipeline
862 flocculation, Journal of Water Process Engineering, 2023, 53.